

Centre Number						Candidate Number				
Surname										
Other Names										
Candidate Signature										

For Examiner's Use	
Examiner's Initials	
Question	Mark
1	
2	
3	
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6	
7	
8	
9	
TOTAL	



General Certificate of Education  
Advanced Subsidiary Examination  
June 2012

# Mathematics

# MPC2

## Unit Pure Core 2

Wednesday 16 May 2012 9.00 am to 10.30 am

**For this paper you must have:**

- the blue AQA booklet of formulae and statistical tables.
- You may use a graphics calculator.

**Time allowed**

- 1 hour 30 minutes

**Instructions**

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- Write the question part reference (eg (a), (b)(i) etc) in the left-hand margin.
- You must answer each question in the space provided for that question. If you require extra space, use an AQA supplementary answer book; do **not** use the space provided for a different question.
- Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

**Information**

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 75.

**Advice**

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- You do not necessarily need to use all the space provided.



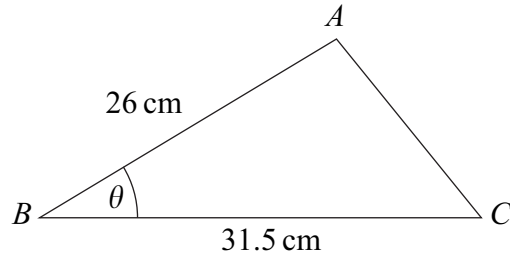
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2

The triangle  $ABC$ , shown in the diagram, is such that  $AB = 26$  cm and  $BC = 31.5$  cm.



The acute angle  $ABC$  is  $\theta$ , where  $\sin \theta = \frac{5}{13}$ .

- (a) Calculate the area of triangle  $ABC$ . (2 marks)
- (b) Find the exact value of  $\cos \theta$ . (1 mark)
- (c) Calculate the length of  $AC$ . (3 marks)

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QUESTION  
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3 (a) Expand  $\left(x^{\frac{3}{2}} - 1\right)^2$ . (2 marks)

(b) Hence find  $\int \left(x^{\frac{3}{2}} - 1\right)^2 dx$ . (3 marks)

(c) Hence find the value of  $\int_1^4 \left(x^{\frac{3}{2}} - 1\right)^2 dx$ . (2 marks)

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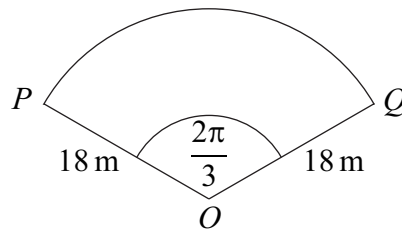
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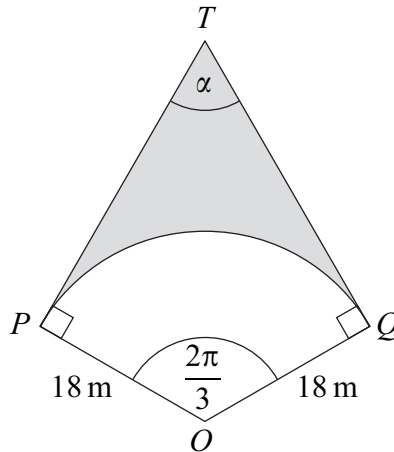


- 5 The diagram shows a sector  $OPQ$  of a circle with centre  $O$ .



The radius of the circle is 18 m and the angle  $POQ$  is  $\frac{2\pi}{3}$  radians.

- (a) Find the length of the arc  $PQ$ , giving your answer as a multiple of  $\pi$ . (2 marks)
- (b) The tangents to the circle at the points  $P$  and  $Q$  meet at the point  $T$ , and the angles  $TPO$  and  $TQO$  are both right angles, as shown in the diagram below.



- (i) Angle  $PTQ = \alpha$  radians. Find  $\alpha$  in terms of  $\pi$ . (1 mark)
- (ii) Find the area of the shaded region bounded by the arc  $PQ$  and the tangents  $TP$  and  $TQ$ , giving your answer to three significant figures. (6 marks)

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**6** At the point  $(x, y)$ , where  $x > 0$ , the gradient of a curve is given by

$$\frac{dy}{dx} = 3x^2 - \frac{4}{x^2} - 11$$

The point  $P(2, 1)$  lies on the curve.

**(a) (i)** Verify that  $\frac{dy}{dx} = 0$  when  $x = 2$ . *(1 mark)*

**(ii)** Find the value of  $\frac{d^2y}{dx^2}$  when  $x = 2$ . *(4 marks)*

**(iii)** Hence state whether  $P$  is a maximum point or a minimum point, giving a reason for your answer. *(1 mark)*

**(b)** Find the equation of the curve. *(4 marks)*

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QUESTION  
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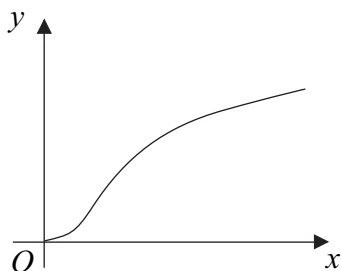
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- 9 The diagram shows part of a curve whose equation is  $y = \log_{10}(x^2 + 1)$ .



- (a) Use the trapezium rule with five ordinates (four strips) to find an approximate value for

$$\int_0^1 \log_{10}(x^2 + 1) dx$$

giving your answer to three significant figures. (4 marks)

- (b) The graph of  $y = 2 \log_{10} x$  can be transformed into the graph of  $y = 1 + 2 \log_{10} x$  by means of a translation. Write down the vector of the translation. (1 mark)

- (c) (i) Show that  $\log_{10}(10x^2) = 1 + 2 \log_{10} x$ . (2 marks)

- (ii) Show that the graph of  $y = 2 \log_{10} x$  can also be transformed into the graph of  $y = 1 + 2 \log_{10} x$  by means of a **stretch**, and describe the stretch. (4 marks)

- (iii) The curve with equation  $y = 1 + 2 \log_{10} x$  intersects the curve  $y = \log_{10}(x^2 + 1)$  at the point  $P$ . Given that the  $x$ -coordinate of  $P$  is positive, find the gradient of the line  $OP$ , where  $O$  is the origin. Give your answer in the form  $\log_{10}\left(\frac{a}{b}\right)$ , where  $a$  and  $b$  are integers. (4 marks)

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QUESTION  
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QUESTION  
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**END OF QUESTIONS**



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